Name: Date:

## Unit 3 REVIEW - Composite, Implicit, and Inverse Functions

Reviews do NOT cover all material from the lessons but should remind you of key points. To be prepared, you should review all packets from Unit 3.

## Find the derivative.

| 1. $h(x)=\cos ^{2}(4 x)$ | 2. $y=\ln \sqrt{x+3}$ |
| :--- | :--- |
|  |  |
| 3. $x^{2}+2 y^{5}=10 x y$ | 4. $y=\csc ^{-1}\left(x^{3}\right)$ |

For each problem, let $f$ and $g$ be differentiable functions where $g(x)=f^{-1}(x)$ for all $x$.
5. $f(6)=-1, f(4)=-2, f^{\prime}(6)=3$, and $f^{\prime}(4)=$ 7. What is the value of $g^{\prime}(-1)$ ?
6. Let $f$ be the function defined by
$f(x)=x^{3}+3 x+1$. Let $g(x)=f^{-1}(x)$, where $g(-3)=-1$. What is the value of $g^{\prime}(-3)$ ?

Find $\frac{d^{2} y}{d x^{2}}$ based on the given information.
7. $y=x^{5}-e^{4 x}$
8. $y=y^{2}+x$
9. Find the equation of the tangent line. $x^{2}+7 y^{2}=8 y^{3}$ at $(-6,2)$
10. If $x=y^{2}-\cos x$ find $\frac{d^{2} y}{d x^{2}}$ at $\left(\frac{\pi}{6}, \frac{1}{2}\right)$.

